

EE359 – Lecture 6 Outline

- **Announcements:**
 - **HW due tomorrow 4pm**
 - **Makeup lecture next Friday, Oct. 20, 10:30-11:50 in this room**
- **Review of Last Lecture**
- **Wideband Multipath Channels**
- **Scattering Function**
- **Multipath Intensity Profile**
- **Doppler Power Spectrum**

Review of Last Lecture

- For $\phi_n \sim U[0, 2\pi]$, $r_I(t), r_Q(t)$ zero mean, WSS, with

$$A_{r_I}(\tau) = P_r E_{\theta_n} [\cos 2\pi f_{D_n} \tau] = A_{r_Q}(\tau), \quad f_{D_n} = v \cos \theta_n / \lambda$$

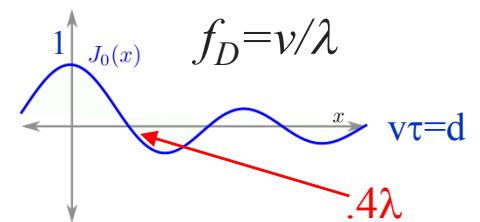
$$A_{r_I, r_Q}(\tau) = P_r E_{\theta_n} [\sin 2\pi f_{D_n} \tau] = -A_{r_I, r_Q}(\tau)$$

- Uniform AoAs in Narrowband Model

- In-phase/quad comps have zero cross correlation and

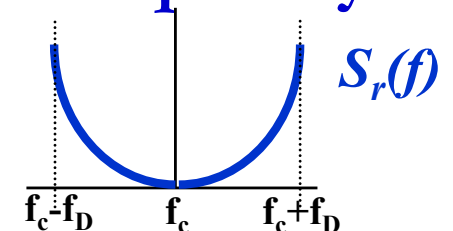
$$A_{r_I}(\tau) = A_{r_Q}(\tau) = P_r J_0(2\pi f_D \tau)$$

Decorrelates over roughly half a wavelength



- PSD maximum at the maximum Doppler frequency

- PSD used to generate simulation values



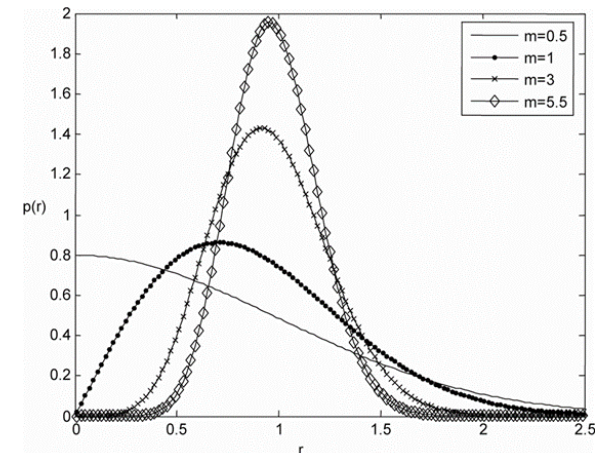
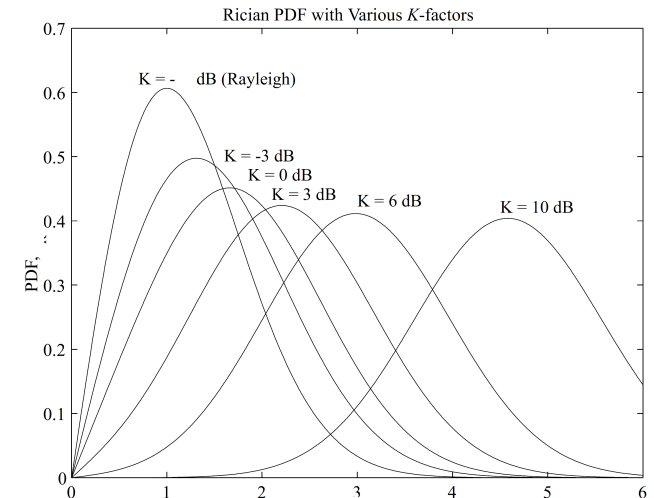
Review Continued:

Signal Envelope Distribution

- CLT approx. leads to Rayleigh distribution (power is exponential)
- When LOS component present, Rician distribution is used

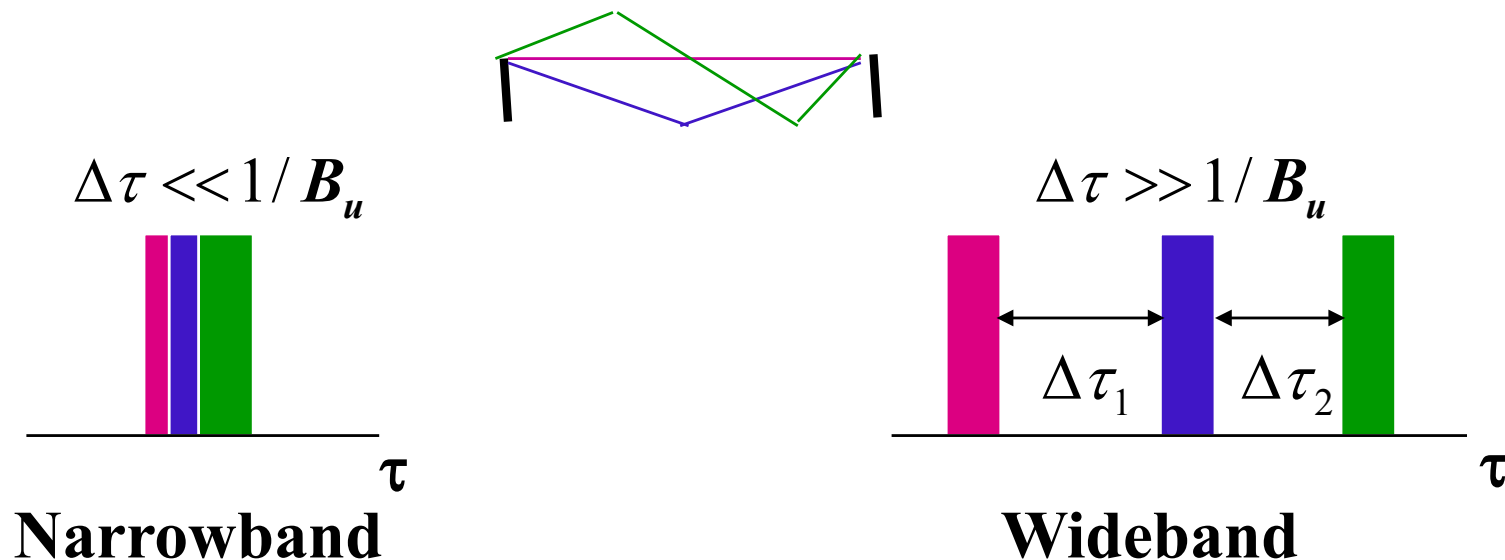
To cover today

- Measurements support Nakagami distribution in some environments
 - Similar to Rician, but models “worse than Rayleigh”
 - Lends itself better to closed form BER expressions



Wideband Channels

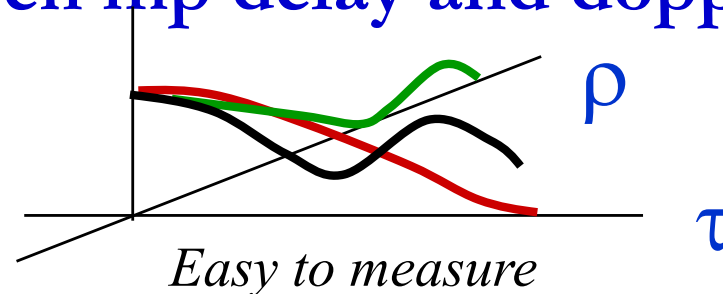
- Individual multipath components resolvable
- True when time difference between components exceeds signal bandwidth
 - High-speed wireless systems are wideband for most environments



Scattering Function

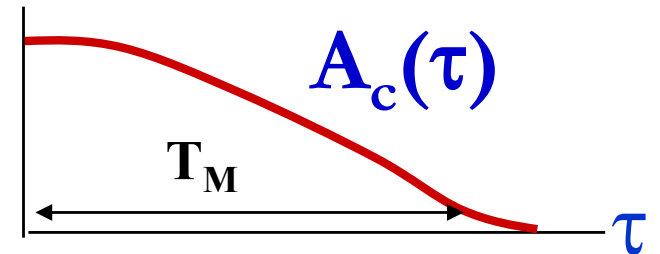
- Typically characterize $c(\tau, t)$ by its statistics, since it is a random process
- Underlying process WSS and Gaussian, so only characterize mean (0) and correlation
- Autocorrelation is $A_c(\tau_1, \tau_2, \Delta t) = A_c(\tau, \Delta t)$
 - Correlation for single mp delay/time difference
- Statistical scattering function:
 - Average power for given mp delay and doppler

$$s(\tau, \rho) = \mathcal{F}_{\Delta t}[A_c(\tau, \Delta t)]$$



Multipath Intensity Profile

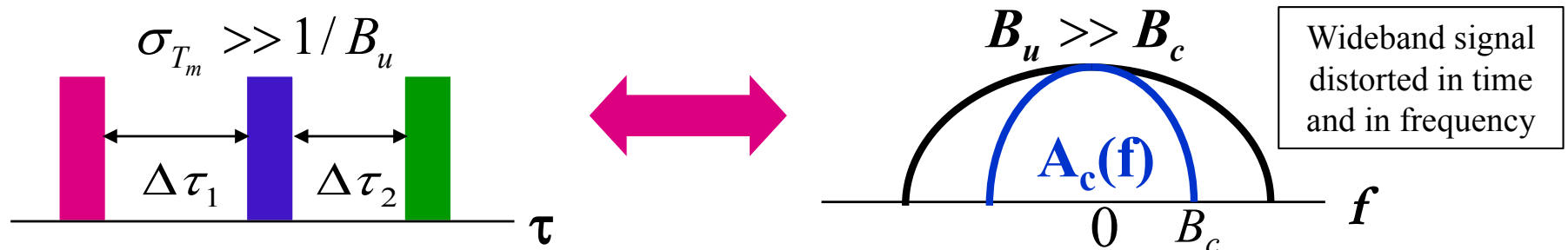
- Defined as $A_c(\tau, \Delta t=0) = A_c(\tau)$



- Determines average (μ_{T_m}) and rms (σ_{T_m}) delay spread
- Approximates maximum delay of significant multipath

- Coherence bandwidth $B_c = 1/\sigma_{T_m}$

- Maximum frequency over which $A_c(\Delta f) = F[A_c(\tau)] > 0$
- $A_c(\Delta f) = 0$ implies signals separated in freq. by Δf will be **uncorrelated** after going through channel: freq. distortion

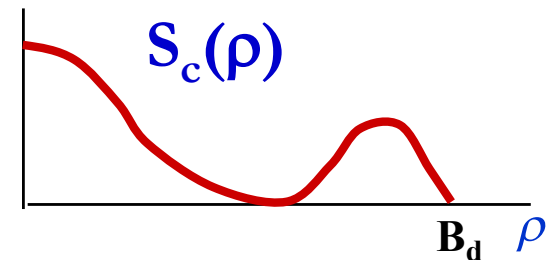


Doppler Power Spectrum

Scattering Function: $s(\tau, \rho) = \mathcal{F}_{\Delta t}[A_c(\tau, \Delta t)]$

- Doppler Power Spectrum: $S_c(\rho) = \mathcal{F}_{\Delta t}[A_c(\Delta f=0, \Delta t) \triangleq A_c(\Delta t)]$

$$A_c(\Delta f, \Delta t) = \mathcal{F}_{\tau}[A_c(\tau, \Delta t)]$$



- Power of multipath at given Doppler
- Doppler spread B_d : Max. doppler for which $S_c(\rho) > 0$.
- Coherence time $T_c = 1/B_d$: Max time over which $A_c(\Delta t) > 0$
 - $A_c(\Delta t) = 0 \Rightarrow$ signals separated in time by Δt uncorrelated after passing through channel
- Why do we look at Doppler w.r.t. $A_c(\Delta f=0, \Delta t)$?
 - Captures Doppler associated with a narrowband signal
 - Autocorrelation over a narrow range of frequencies
 - Fully captures time-variations, multipath angles of arrival

Main Points

- **Wideband channels have resolvable multipath**
 - Statistically characterize $c(\tau, t)$ for WSSUS model
 - Scattering function characterizes rms delay and Doppler spread. Key parameters for system design.
- **Delay spread defines maximum delay of significant multipath components. Inverse is coherence BW**
 - Signal distortion in time/freq. when delay spread exceeds inverse signal BW (signal BW exceeds coherence BW)
- **Doppler spread defines maximum nonzero doppler, its inverse is coherence time**
 - Channel decorrelates over channel coherence time